

# Assessing and Communicating Heterogeneity of Treatment Effects (HTE) for Patient Subpopulations: Challenges and Opportunities

## Subgroup Identification The Hardest Problem There Is

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# Outline

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Clinical Trials

Observational Data

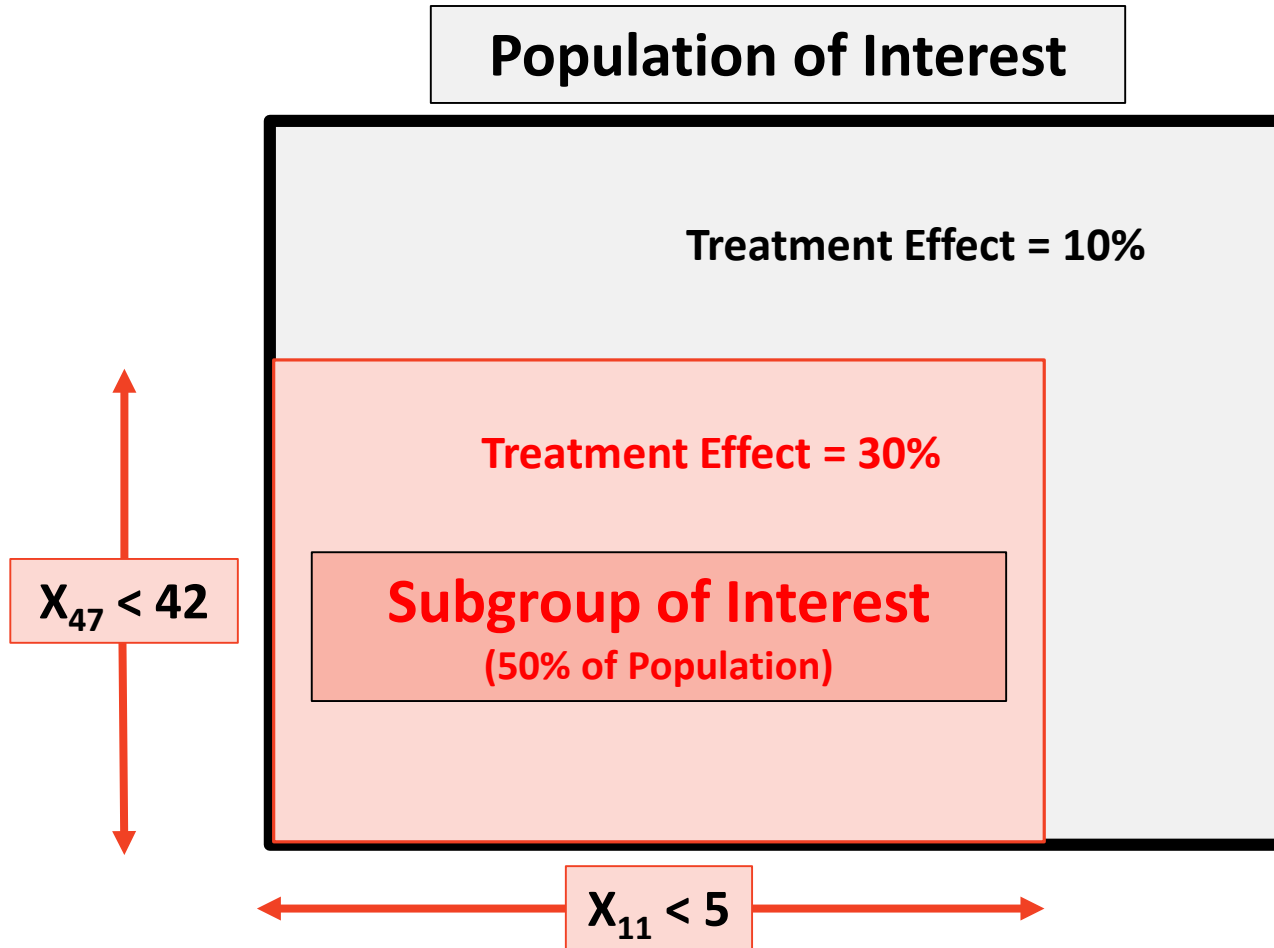
What We Can Do Now



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# Clinical Trials

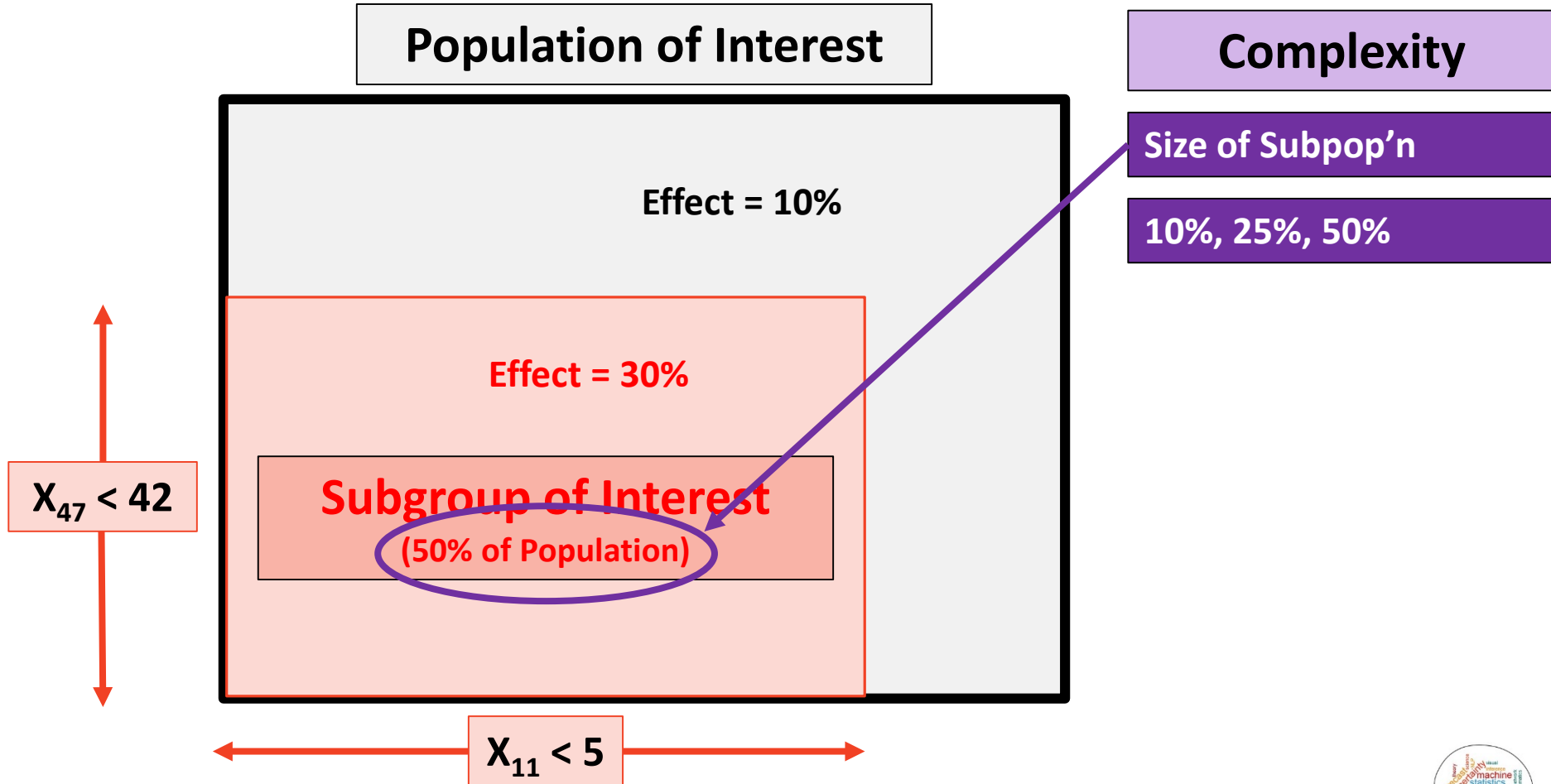
## Treatment versus Control



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# Clinical Trials

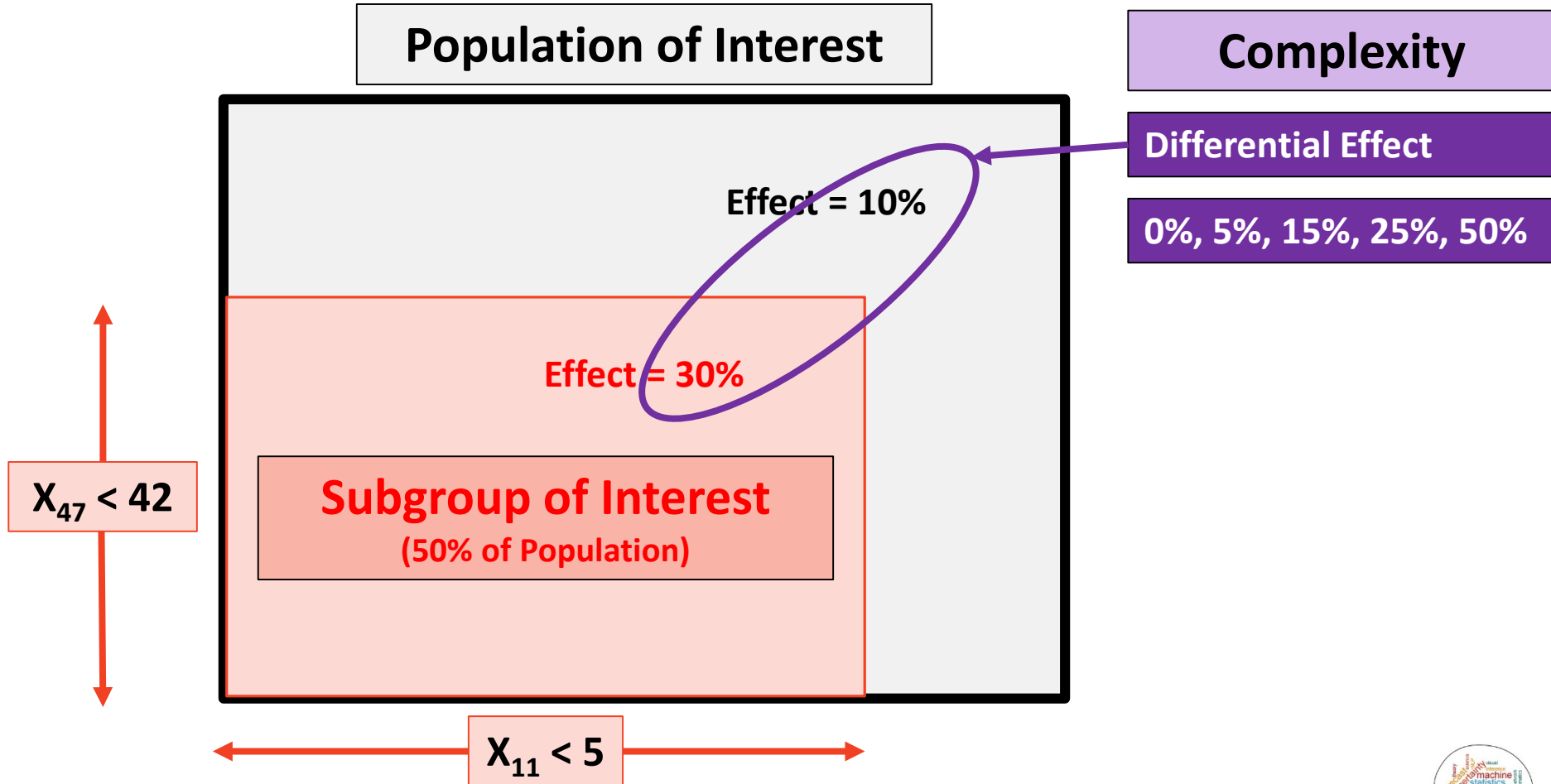
## Treatment versus Control



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# Clinical Trials

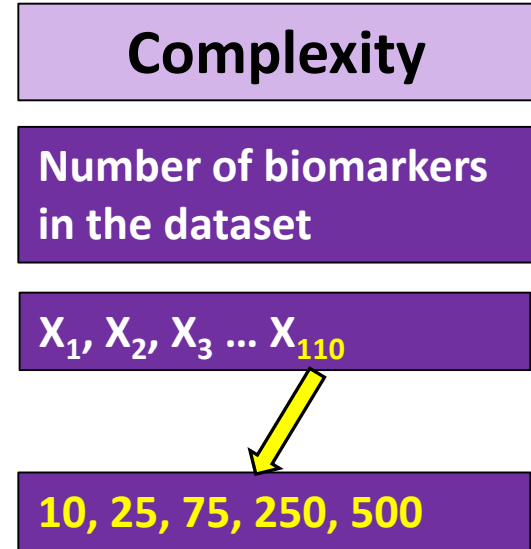
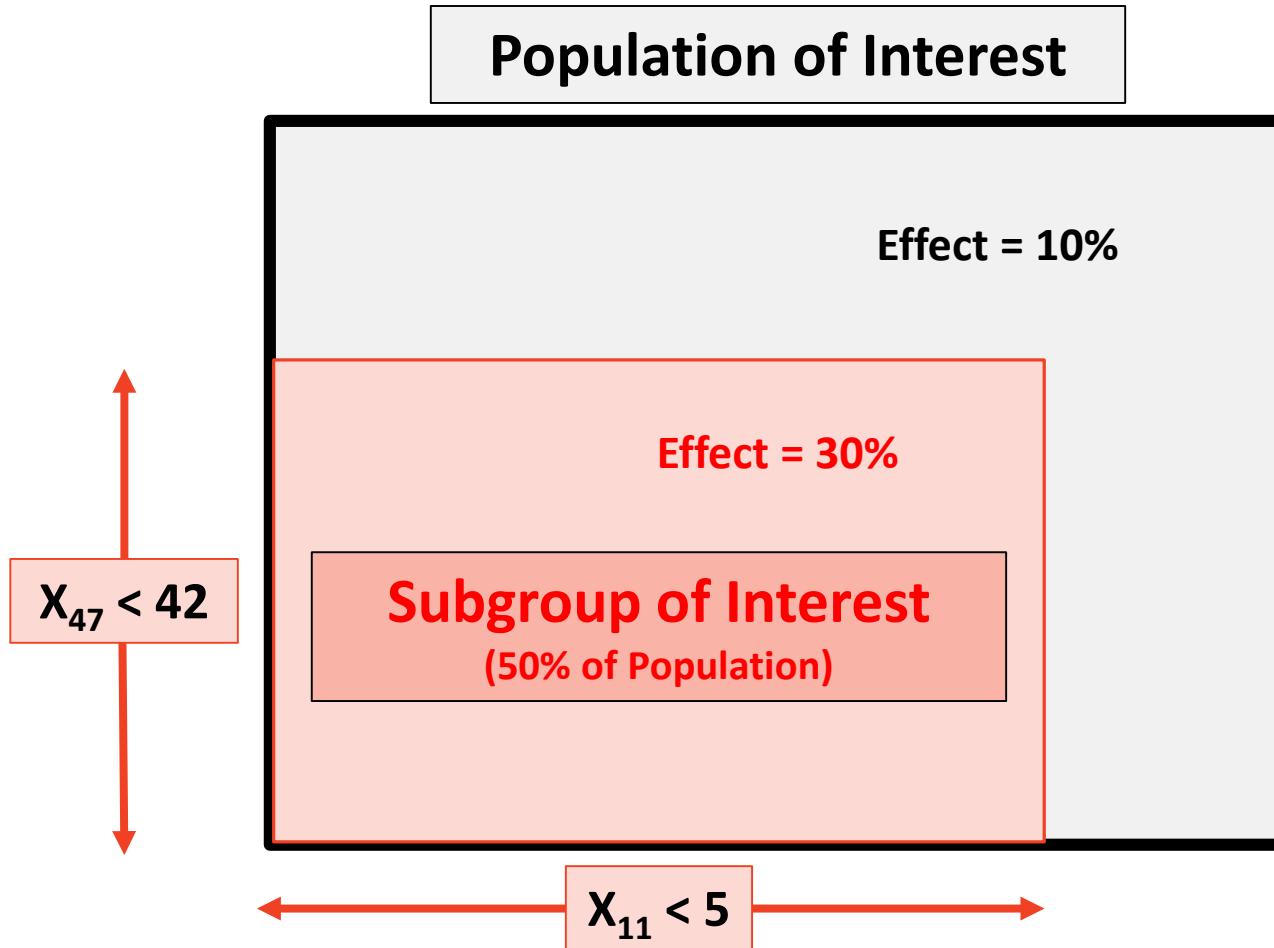
## Treatment versus Control



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# Clinical Trials

## Treatment versus Control



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# Clinical Trials

## Treatment versus Control

Population of Interest

Complexity

Number of biomarkers  
defining subpop'n

1, 2

Effect = 10%

Effect = 30%

Subgroup of Interest  
(50% of Population)

$X_{47} < 42$

$X_{11} < 5$

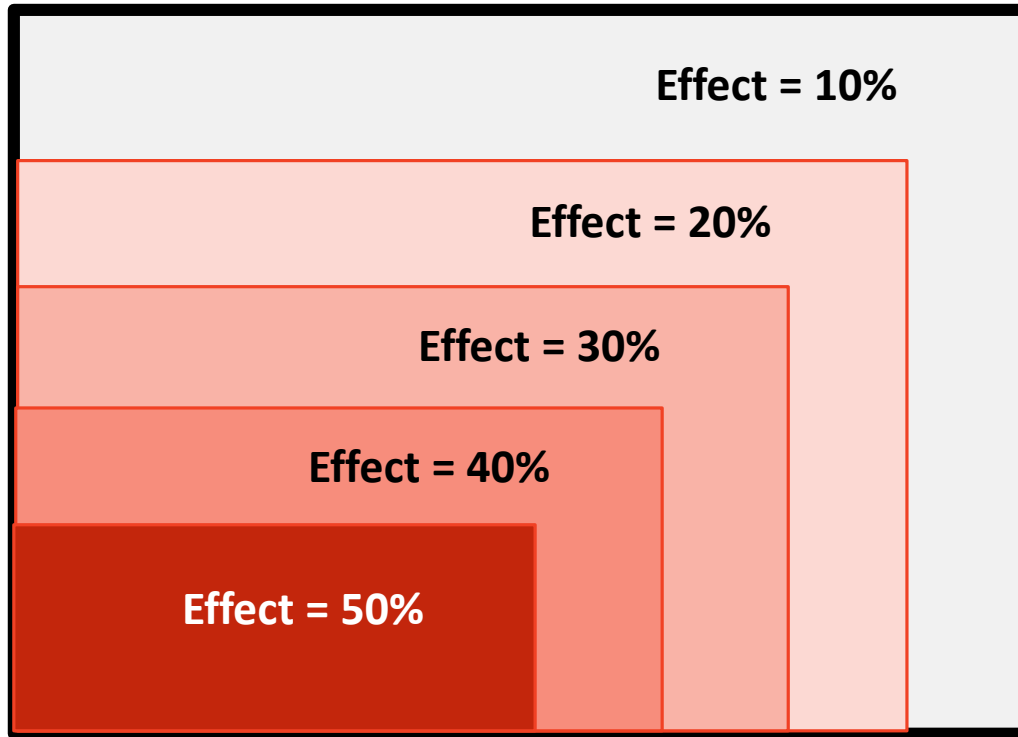


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# Clinical Trials

## Treatment versus Control

Population of Interest



$X_{47} < 42$

$X_{11} < 5$

Complexity

Nature of biomarkers  
effect

1, 2

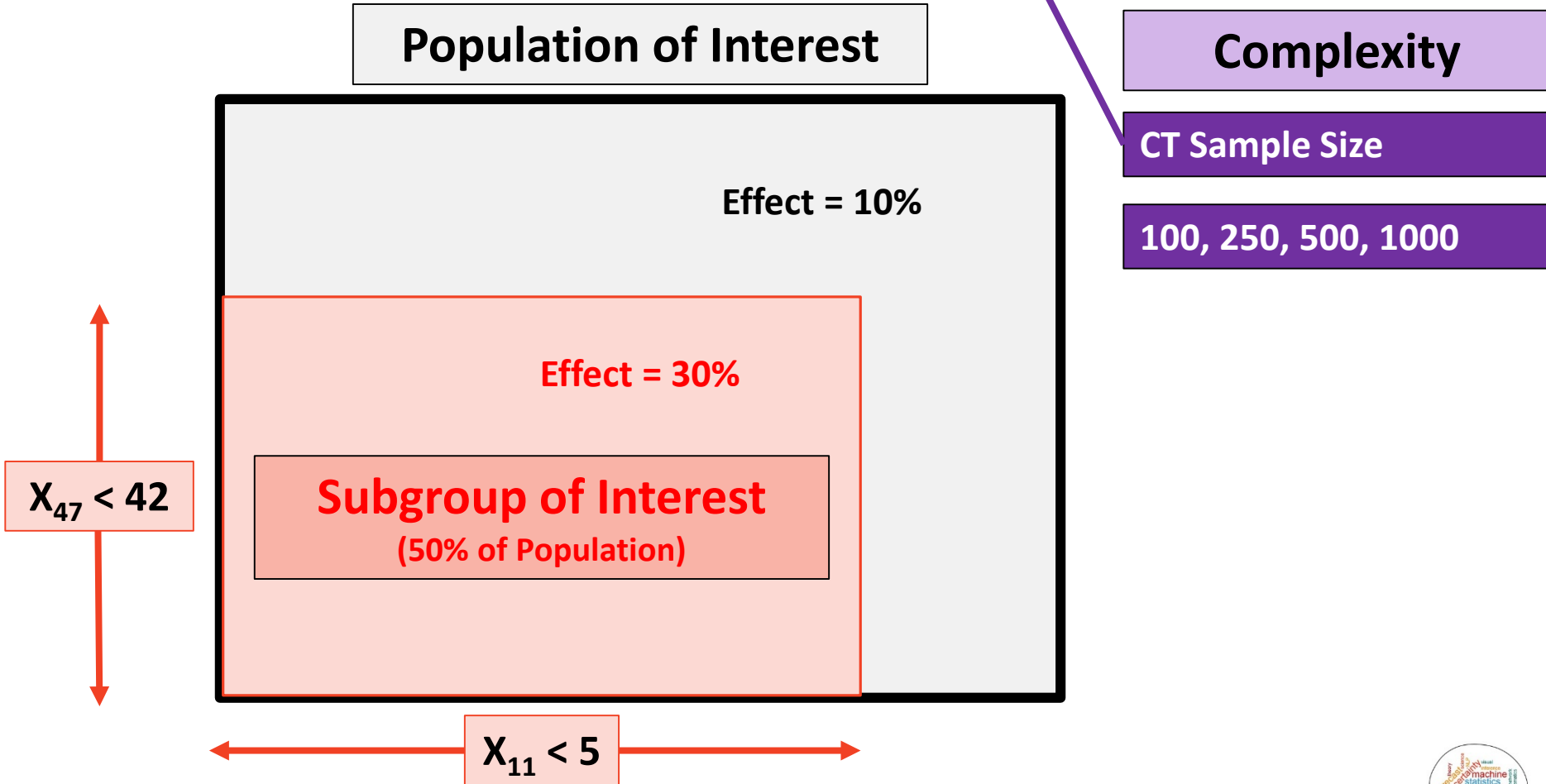


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# Clinical Trials

## Treatment versus Control



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# Subgroup Identification Challenge

Scenarios (i.e. combinations of possibilities)

$3 \times 5 \times 5 \times 2 \times 2 \times 4 = 1200$  !!!

Simulated 1200 datasets with these known parameters.

Posted on *Innocentive* and challenged the world ...

**FIND THE SUBGROUP (i.e. the X's and the cut-offs)**

Created a scoring system to rank solutions (0, 100).

Participants could make 1 attempt per day over 3 months.

# Subgroup Identification Challenge

Total of 748 entered the competition

- USA 279, India 69, UK 49, Canada 43, Germany 24, Australia 20, Russia 20, Italy 19, Spain 16,

**62/120 (52%) did no better than flipping a coin !!!**

- + 39 other countries (including Seychelles!)

Only 120 submitted a valid solution (that could be scored)



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# Subgroup Identification Challenge

Internal benchmark score = 62

- This problem is very hard !!

Only two submissions did marginally better with scores of 64 and 65.

- 118/120 (98%) did worse than the internal benchmark



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# Clinical Trials

## Treatment versus Control

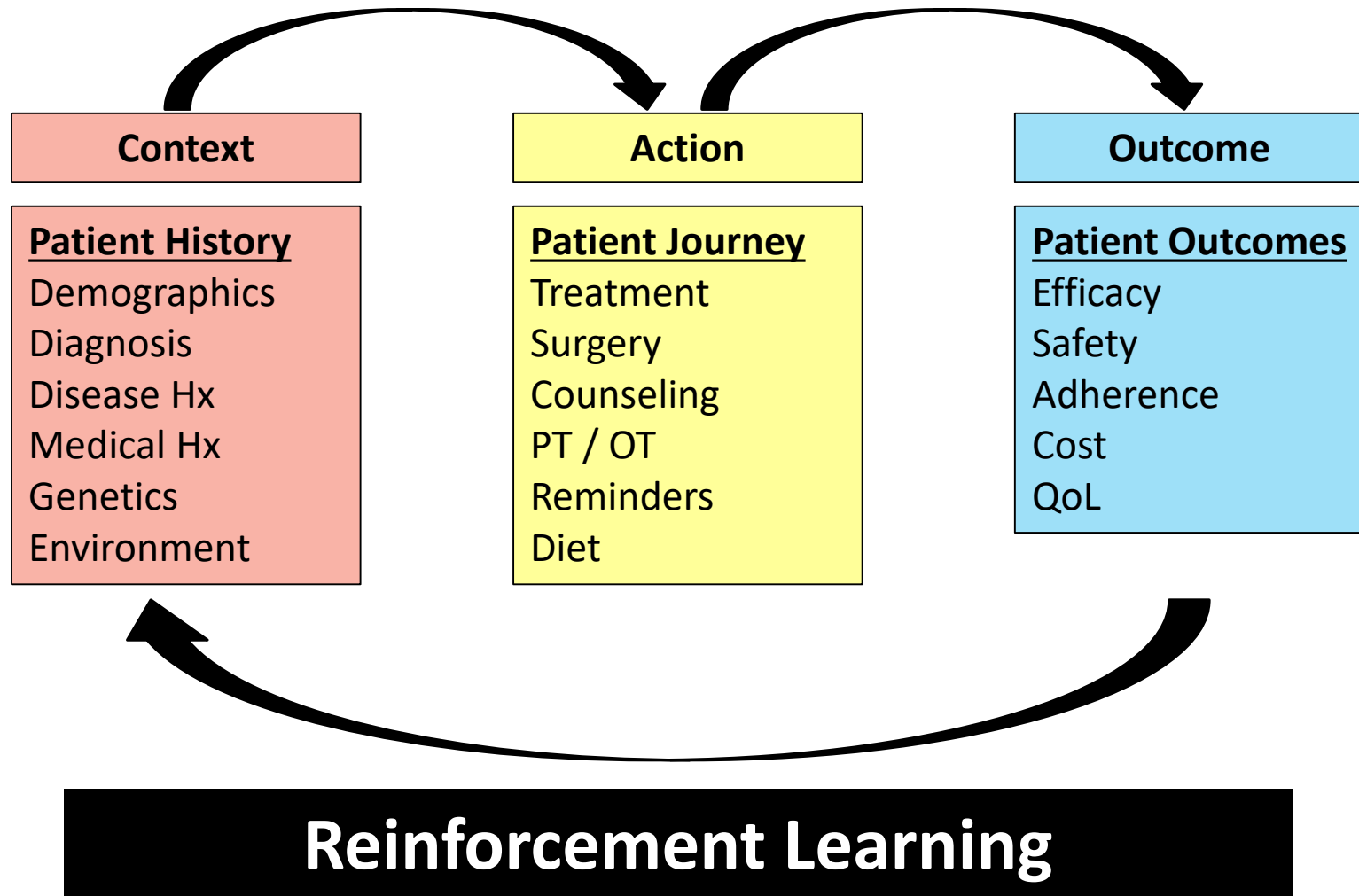
### Conclusion

Even with randomized, controlled trials/data, under normal circumstances (i.e. reasonable parameter values) and simple biomarkers relationships to response, **the subgroup is not identified or mis-identified a high percentage of the time.**



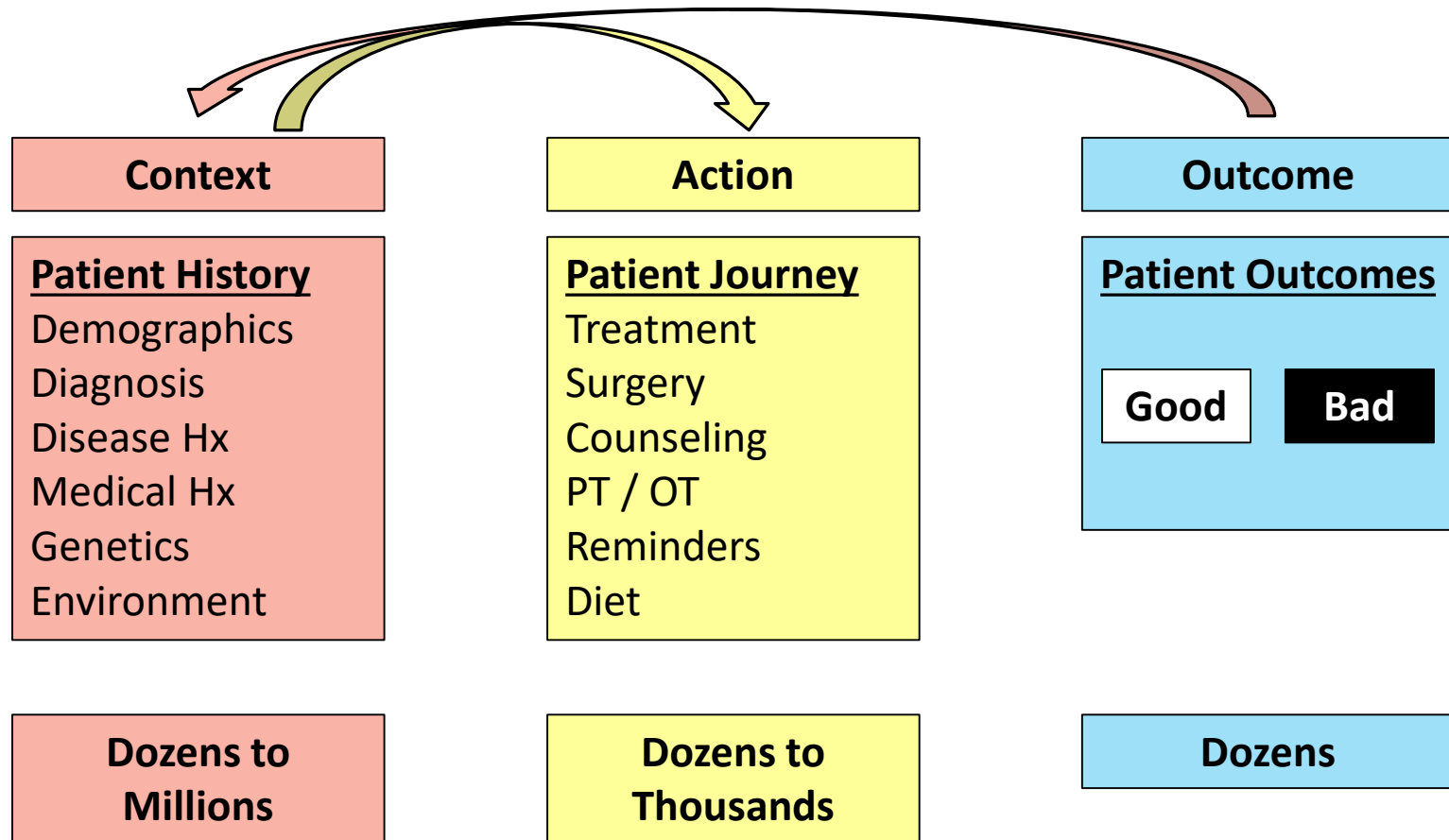
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# Observational Data



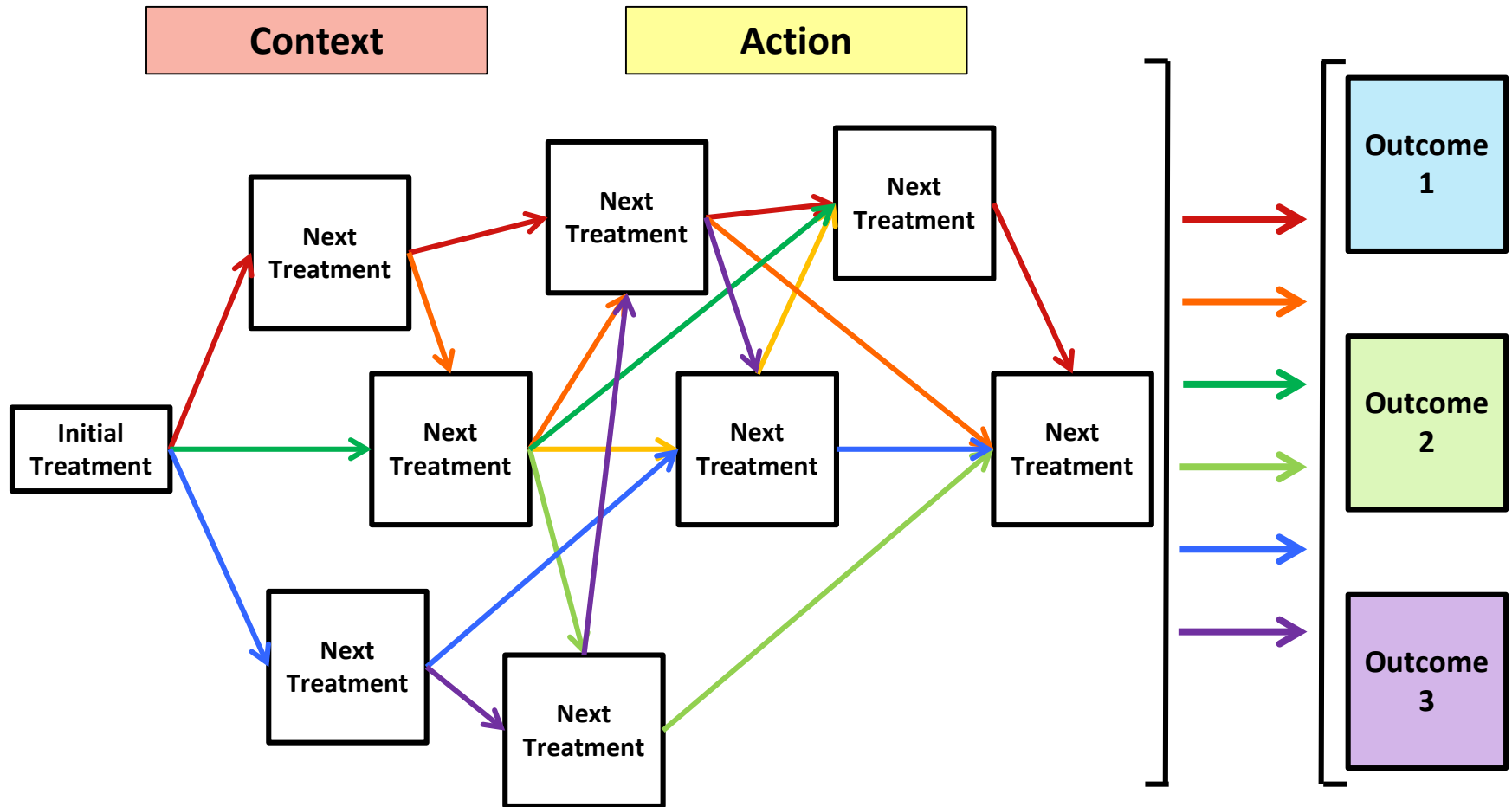
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# Observational Data



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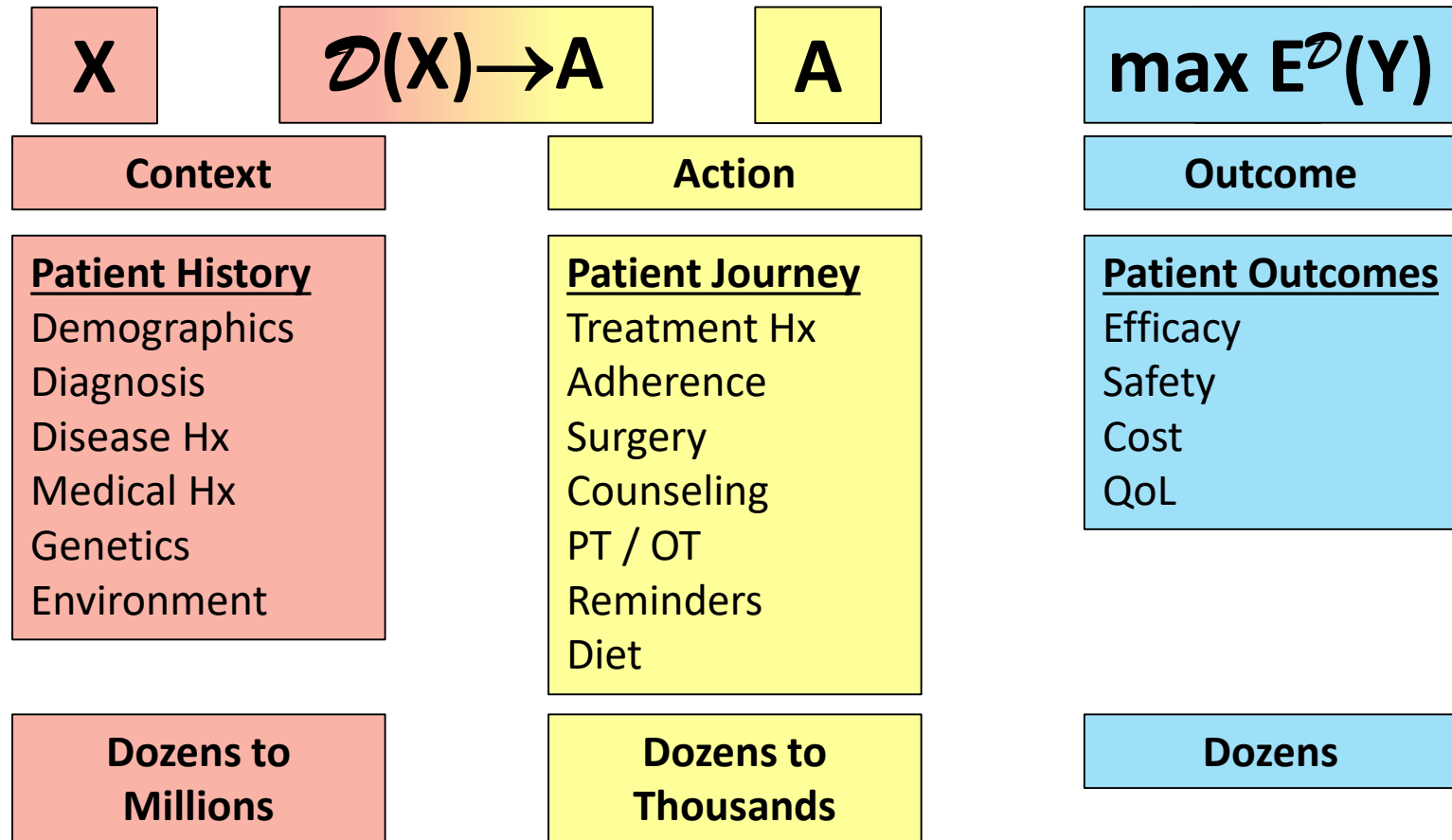
# Observational Data







# Individualized Treatment Regimes



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# Individualized Treatment Regimes

Define,

$$E^{\mathcal{D}}(Y) = \int Y d\mathcal{P}^{\mathcal{D}} = \int Y \frac{d\mathcal{P}^{\mathcal{D}}}{d\mathcal{P}} d\mathcal{P} = E \left[ \frac{I\{A = \mathcal{D}(X)\}}{p(A|X)} Y \right],$$

where we use the fact that,

$$\frac{d\mathcal{P}^{\mathcal{D}}}{d\mathcal{P}} = \frac{p(y|x, a) I\{a = \mathcal{D}(x)\} p(x)}{p(y|x, a) p(a|x) p(x)} = \frac{I\{a = \mathcal{D}(x)\}}{p(a|x)}.$$

Our objective is to find  $\mathcal{D}(\cdot)$  to maximize the following value function:

Value function

$$\mathcal{D}_o \in \operatorname{argmax}_{\mathcal{D} \in R} E^{\mathcal{D}}(Y) = E \left[ \frac{I\{A = \mathcal{D}(X)\}}{p(A|X)} Y \right], \quad (1)$$

where  $R$  is a space of possible treatment recommendations.

# Observational Data

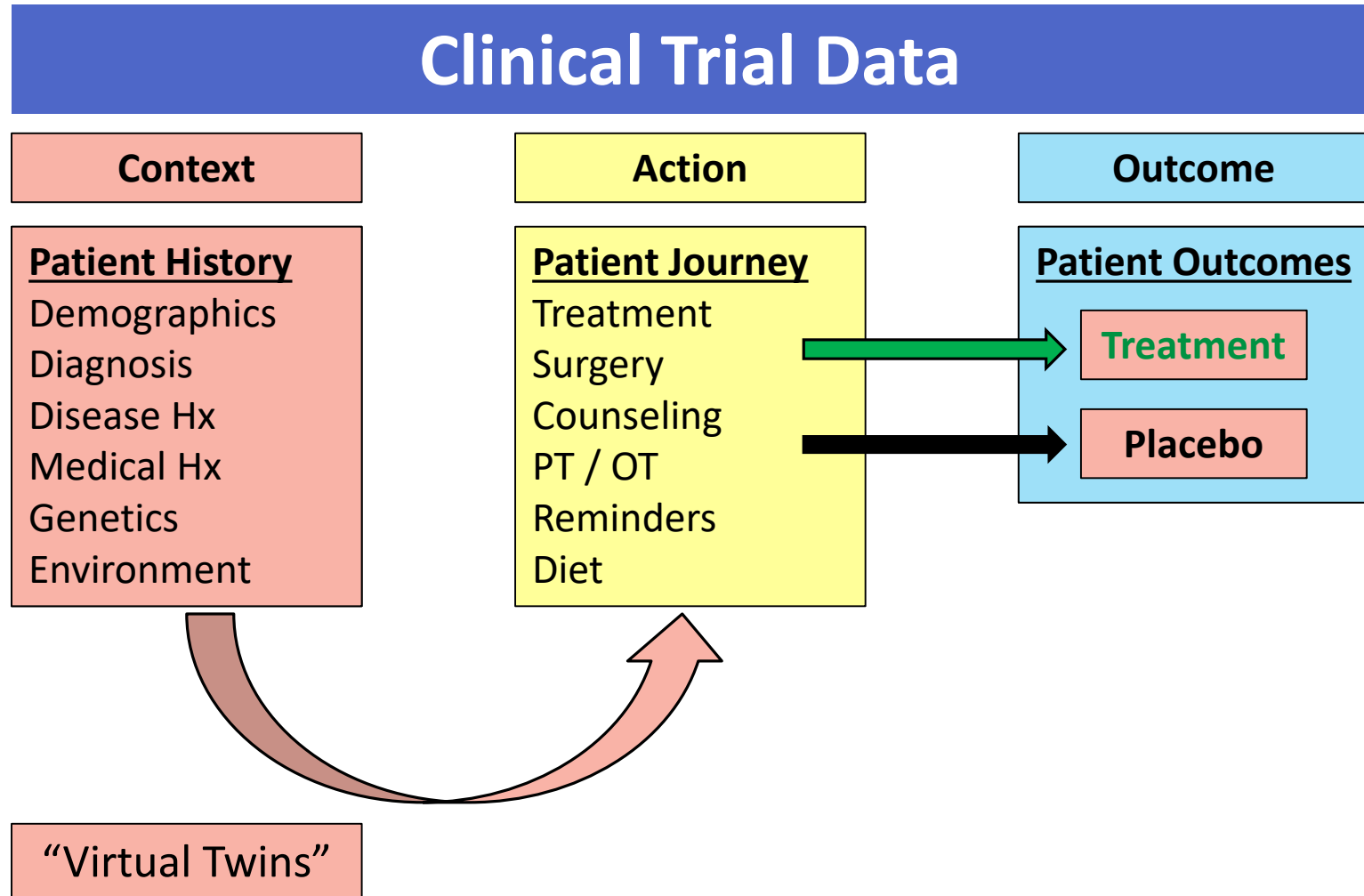
## Conclusion

- ITR is an emerging (promising?) methodology.
- It can help find the right  $\mathcal{D}(X)$  within the context of available decisions and covariates.
- Use artificial intelligence (i.e. reinforcement learning algorithms) to help solve this problem.



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# What Can We Do Now?



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# What Can We Do Now?

## Imagine an App



“Here are the 50 patients in the clinical trials database most like you.”

Review of summary Context data.

“Here are the treatments and doses that they took in the clinical trials.”

Review of summary Action data.

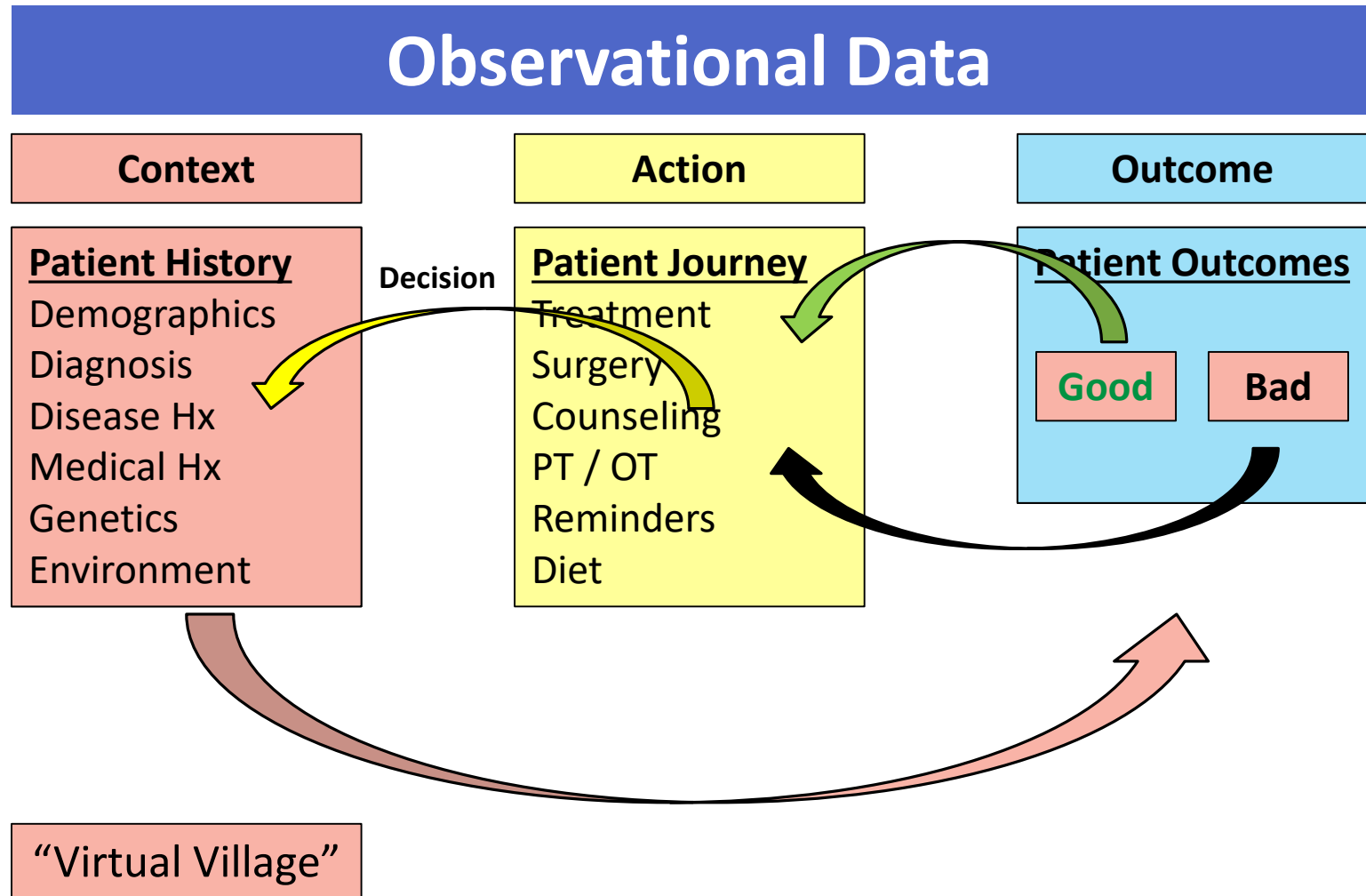
“Here are the primary efficacy and safety summaries.”

Review of summary Outcome data.



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# What Can We Do Now?



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# What Can We Do Now?

## Imagine an App





# What Can We Do Now?

Initially done with CT data from approval.

- Could FDA do this?

Extend to observational data?

- Embed in Electronic Medical Records?
- Create recommender system (e.g. Netflix ...)

**CREATE PATIENT-CENTERED SUBGROUPS! (?)**

**Probabilize** efficacy and safety outcomes

- Patient use their own utility function



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# Conclusion

**THE** problem of this era is ...

Finding the few actionable X's (out of many, many X's) that predict favorable outcomes for INDIVIDUAL PATIENTS.

- It is extremely difficult.
- Having the ***right data*** with ***very smart analytics*** is the key.



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# Conclusion

“**My ultimate dream** would be to find signatures of high-responding patients through this kind of artificial intelligence, and prospectively identify: Who will be the super-responders? ... If we can master that — that would be a great longer-term win.”

Vas Narasimhan, MD  
CEO, Novartis  
Oct 29, 2018



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# Multiplicity and Bayes

## Multiplicity

What is the probability that my finding in real or chance (i.e. spurious)?

## Bayes

Quantifying the probability of a hypothesis



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# Multiplicity and Bayes

## Solanezumab – EXPEDITION STUDIES

**The following is a Steve Ruberg analysis (post hoc).**

**It explicitly does not use information from Lilly.**

**It is meant solely to be illustrative and does not represent what analyses were done by Lilly, which were much more sophisticated than presented here, or how decisions were made by Lilly.**



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# Multiplicity and Bayes

Suppose our prior probability that Solanezumab works is 0.30 (i.e. the null hypothesis is false).

There are 5 hypotheses of interest:

- The overall population (primary)
- Mild population
- Moderate population
- *APOE*  $\epsilon$ 4 carriers
- *APOE*  $\epsilon$ 4 non-carriers



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# Multiplicity and Bayes

Split the prior (0.30) across the five hypotheses of interest.

1. Give most of the probability (0.14) to the Overall population.
2. Divvy the remaining probability to the other subpopulations
  - a) Equally – i.e.  $0.16/4 = 0.04$
  - b) Weighted – i.e. give larger prior (0.06) to Mild and *APOE* ε4 carriers



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# Multiplicity and Bayes

| Hypothesis            | Prior<br>(version A) | Prior<br>(version B) |
|-----------------------|----------------------|----------------------|
| Overall               | 0.14                 | 0.14                 |
| Mild                  | 0.04                 | 0.06                 |
| Moderate              | 0.04                 | 0.02                 |
| APOE $\epsilon$ 4 (+) | 0.04                 | 0.06                 |
| APOE $\epsilon$ 4 (-) | 0.04                 | 0.02                 |
| <b>Total</b>          | <b>0.30</b>          | <b>0.30</b>          |



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# Multiplicity and Bayes

| Hypothesis            | Prior<br>(version A) | Prior<br>(version B) |
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| <b>Total</b>          | <b>0.30</b>          | <b>0.30</b>          |



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# Multiplicity and Bayes

## EXPEDITION 1 (Mild and Moderate AD Patients)

### ADAS-Cog11

- Overall:  $p=0.24$
- Mild:  $p=0.008$

### ADAS-Cog14

- Mild:  $p=0.003$

Is the finding in Mild  
patients real or  
spurious?

Doody, Rachele S. et al. "Phase 3 Trials of Solanezumab for Mild-to-Moderate Alzheimer's Disease." N Engl J Med 2014; 370:311-321. (with Supplementary Appendix)



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# Multiplicity and Bayes

**EXPEDITION 1**  
(Mild and Moderate  
AD Patients)

**ADAS-Cog11**

- Overall:  $p=0.24$
- Mild:  $p=0.008$

**ADAS-Cog14**

- Mild:  $p=0.003$

**MILD PATIENTS**

| ADAS-Cog11    |         |             |
|---------------|---------|-------------|
| Initial Prior | P-value | Posterior * |
| 0.04          | 0.008   | 0.28        |
| 0.06          | 0.008   | 0.38        |

\* Using Bayes Factor:  $O_0 \times [-e \times p \times \ln(p)] \leq O_1$



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# Multiplicity and Bayes

**EXPEDITION 1**  
(Mild and Moderate  
AD Patients)

## ADAS-Cog11

- Overall:  $p=0.24$
- Mild:  $p=0.008$

## ADAS-Cog14

- Mild:  $p=0.003$

## MILD PATIENTS

| ADAS-Cog11    |         |             |               |         |             |
|---------------|---------|-------------|---------------|---------|-------------|
| Initial Prior | P-value | Posterior * | Revised Prior | P-value | Posterior * |
| 0.04          | 0.008   | 0.28        | 0.02          | 0.008   | 0.16        |
| 0.06          | 0.008   | 0.38        | 0.03          | 0.008   | 0.23        |
| ADAS-Cog14    |         |             |               |         |             |
|               |         |             | 0.02          | 0.003   | 0.30        |
|               |         |             | 0.03          | 0.003   | 0.39        |



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